Efficient On-Line Mining of Large Databases

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Abstract: Research in data mining has made many efforts to apply various mining algorithms efficiently on large databases. However, a serious problem in their practical application is the long processing time of such algorithms. This paper presents a framework for mining large databases without size limit in acceptable processing times. We achieve our first objective by integrating data mining algorithms, especially decision tree-based methods, within Database Management Systems (DBMSs). We are thus only limited by disk capacity, and not by available main memory. However, the disk accesses that are necessary to scan the database induce long response times when it is very large. To improve processing times and carry out our second objective, we exploit some structures and primitives provided by SQL engines for data retrieval. We propose two types of optimizations. In the first, we reduce the size of the learning database by building its corresponding contingency table. In this case, the decision tree methods deal with this contingency table rather than with the whole training set. Our second optimization proposal consists in reducing the number of database accesses by exploiting bitmap indices. Then again, the decision tree methods deal with bitmap indices rather than with the whole training set. To validate our approach, we implemented various decision tree-based methods within the Oracle DBMS. We observed that our contingency table-based and bitmap index-based methods allowed to process bigger databases than in-memory implementations while presenting linear processing times.

Keywords: Databases, on-line data mining, decision trees, performance, relational views, contingency table, bitmap indices.

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1 Introduction

The input of traditional data mining algorithms are data structured as attribute-value tables. Since these algorithms operate in main memory, the size of the processed databases is limited. Nowadays, one of the key challenges in Knowledge Discovery in Databases (KDD) is to integrate data mining methods within the framework of traditional database systems so that their implementations can take advantage of the efficiency provided by SQL engines (7).

Data mining and databases should indeed not remain separate components in decision support systems. Integrating data mining tools into Database Management Systems (DBMSs) is a promising research direction for the following reasons.

- Data mining tools need integrated, consistent, and cleaned data. A database is precisely constructed through such preprocessing steps.
- Data mining algorithms operate in main memory, which limits the size of the processed databases. DBMSs provide a framework to manage large databases without size limit, theoretically.
- Some of the more popular data mining algorithms, namely decision tree methods, compute many successive frequencies to build trees. The SQL language includes COUNT and GROUP BY commands to easily compute such frequencies. Moreover, the use of indices can improve data access time when processing the database.
- When data warehouses have been stored into relational databases, On-Line Analytical Processing (OLAP) has been integrated within DBMSs. In the same way, we propose to extend DBMSs’ analysis features with on-line data mining tools.

In this paper, we propose a full integrated solution for mining large databases within DBMSs. We aim at the following two main objectives: (1) mine very large databases without size limit and (2) achieve acceptable processing times. Moreover, in opposition to the integrated approaches proposed in the literature, our approach also presents two main advantages: no extension of the SQL language is needed and no programming through an API (Application Programming Interface) is required. We achieve our first objective by integrating data mining algorithms, especially decision tree-based methods, within DBMSs. However, processing times are quite long. To improve processing time and carry out our second objective, we efficiently exploit some structures and primitives provided by SQL engines for data retrieval.

In our approach, we propose three integrated methods: a view-based method (7), a contingency table-based method (7) and a bitmap index-based method (7). Each method is based on a specific database tool.

1. **View-based method**: Decision tree methods generate a tree (or more generally a graph) that is a succession of smaller and smaller partitions of an initial
training set (table or view). Our key idea comes from this very definition. Indeed, we can make an analogy between building successive, related partitions and creating successive, related relational views. Each node of the decision tree is then associated to the corresponding view. Then, to build the decision tree, we only need relational views that we exploit through SQL queries. We show that we can process very large databases with this method, theoretically without any size limit, while classical, in-memory data mining software cannot. However, processing times are quite long because of multiple accesses to the database.

2. **Contingency table-based method**: In order to improve processing times, preparing the data before the data mining process becomes crucial. We propose an original method to achieve this goal, which consists in reducing the size of the training set. We build a contingency table, i.e., a table that contains the frequencies, corresponding to the whole training set, and whose size is normally much smaller than the table containing the whole training set. Data mining methods are then adapted so that they can apply to this contingency table. To the best of our knowledge, no data mining method currently uses such a data preparation phase.

3. **Bitmap index-based method**: Another method for improving processing times consists in reducing the number of data accesses within the DBMS. The method we propose exploits database indices, namely bitmap indices that have many useful properties, such as count and bit-wise operations that we exploit through SQL queries to build decision trees. Our method presents an important advantage because there is no need to access the source data, since we deal with bitmap indices rather than with the whole training set.

We implemented different decision tree algorithms such as ID3, C4.5 and CART following our three methods within the Oracle DBMS, as PL/SQL stored procedures. In this paper, we detail the algorithm and performance results for the ID3 method, that are quite similar than those of C4.5 and CART. We observe that our integrated approach allows to process larger databases than in-memory implementations while presenting interesting processing times.

This paper expands our previous work along four axes. First, our motivation in this paper is to globally present our integrated approach as a whole. Second, we present a complete overview of the existing approaches for mining large databases from both the data mining and the database fields and compare them to our solution. Third, we detail implementation issues. Finally, we present new experiments on several data sets and discuss the results we obtained when comparing our three integrated methods.

The remainder of this paper is organized as follows. First, we discuss the related work regarding large databases mining in Section 2. Section 3 presents the principles of decision tree-based methods. In sections 4, 5 and 6, we respectively detail our different integrated methods and present their implementation, as well as complexity studies. We also present in section 7 the experiments we performed to validate our approach. We finally conclude this paper and discuss research perspectives in Section 8.
2 Related work

Efficiently mining large databases has been the subject of many research studies for several years. Since traditional data mining algorithms operate in main memory, the size of the processed databases is limited. Different approaches have emerged to overcome this limit. The first one consists in preprocessing data to reduce the size of the learning databases. The second one uses optimization techniques to assure the methods’ scalability. The third one develops tools for integrating data mining algorithms into DBMSs.

2.1 Data preprocessing

Variable and feature selection have become the focus of much research in areas of application for which datasets with tens or hundreds of thousands of variables are available. The objective of variable selection is to improve the prediction performance of the predictors. In fact, it consists in exploiting data preprocessing techniques. First, feature selection (¿, ¿) aims at reducing the number of predictive attributes. The feature selection must assume that the attributes that are deleted from the learning population do not impact the learning result, i.e., it must delete the less pertinent attributes for learning. Sampling techniques (¿, ¿, ¿) aim at considering fewer individuals for learning. The main objective is to obtain a sampling of the learning population that is representative of the whole population. However, the learning quality must not be decreased. It has indeed been proved that, with a well chosen sampling, decision tree algorithms can provide better results than with the whole learning population (¿).

2.2 Scalability

Data mining often induces problems of combinatorial explosion in terms of space and time. Thus, there has been an impressive amount of work related to scalability, which focuses on scaling data mining techniques to work on large datasets. Scalability is achieved by two means:

- optimizing the algorithms (¿, ¿, ¿), i.e., exploring how to improve the efficiency of the mining algorithms;
- optimizing data accesses (¿, ¿, ¿), i.e., focusing on the impact of representation, organization, and access to data on mining algorithms performance.

2.3 Integrated methods

Recently, a new approach has emerged to apply data mining algorithms on large databases. It consists in integrating data mining methods within DBMSs (¿). A first step in this integration process has been achieved with the rise of data warehousing, whose primary purpose is decision support rather than reliable storage. A closely related area is On-Line Analytical Processing (OLAP) (¿). Database vendors also recently integrated data mining methods into their systems under the
form of “black box” tools, either by developing extensions of SQL or by developing
ad-hoc APIs (? , ? ). These tools allow client applications to explore and manipulate
existing mining models and their applications through an interface similar to that
used for exploring tables, views and other first-class relational objects.

Many other integrated approaches have been proposed in the literature. They
usually use either extensions of SQL for developing new operators (? , ? , ?), new
languages (? , ? , ? , ? , ? , ? , ?) or extensions of the DBMS itself by introducing the
concept of “virtual mining view” (?).

There are also advances in the context of integrated approaches that do not
use any API nor extensions of SQL. A new index type has indeed been proposed
(?). It can be considered as an extension of bitmap indices and helps improving
subset searching in large databases. This approach could be used in the field of
association rule mining. Moreover, in (?) the author proposes to integrate the
K-Means clustering method with a relational DBMS using SQL.

In conclusion, integrating data mining algorithms within the framework of tra-
tditional database systems becomes one of the key challenges for research in both
the database and the data mining fields (?). Indeed, it provides on-line data mining
operators to users in addition to usual SQL operators.

3 Decision tree-based methods

3.1 Principle

Decision trees are among the most popular supervised learning methods pro-
posed in the literature. They are appreciated for their simplicity and the high
efficiency of their algorithms, for their ease of use and for the easily interpretable
results they provide. Many induction tree methods have been proposed so far in
the literature. Some, such as ‘Induction Decision Tree’ (ID3) (?) and C4.5 (?),
buid n-ary trees. Others such as ‘Classification And Regression Tree’ (CART) (?),
produce binary trees.

An induction tree may be viewed as a succession of smaller and smaller partitions
of an initial training set. It takes as input a set of objects (tuples) described by a
collection of attributes. Each object belongs to one of a set of mutually exclusive
classes. The induction task determines the class of any object from the values of
its attributes. A training set of objects whose class is known is needed to build
the induction graph. Hence, an induction graph building method takes as input a
set of objects defined by predictive attributes and a class attribute, which is the
attribute to predict.

Decision tree construction methods apply successive criteria on the training
population to obtain these partitions, wherein the size of one class is maximized.
In the ID3 algorithm, for example, the discriminating power of an attribute for
splitting a node of the decision tree is expressed by a variation of entropy. The
entropy $h_s$ of a node $s_k$ (more precisely, its entropy of Shannon) is:

$$ h_s(s_k) = - \sum_{i=1}^{c} \frac{n_{ik}}{n_k} \log_2 \frac{n_{ik}}{n_k} $$ (1)
where \( n_k \) is the frequency of \( s_k \) and \( n_{ij} \) the number of objects of \( s_k \) that belong to class \( C_i \). The information carried by a partition \( S_K \) of \( K \) nodes is then the weighted average of the entropies:

\[
E(S_K) = \sum_{k=1}^{K} \frac{n_k}{n_j} h_s(s_k)
\]

where \( n_j \) is the frequency of the splitted node \( s_j \). Finally, the information gain associated to \( S_K \) is

\[
G(S_K) = h_s(s_j) - E(S_K)
\]

Figure 1 provides an example of decision tree with its associated rules, where \( p(\text{Class } #1) \) is the probability of objects to belong to Class #1.

3.2 Running example

To illustrate how the different methods presented in this paper operate, we use as an example the TITANIC database (Table 1), which is a training set of 2201 tuples. It is commonly used to test decision tree building methods.

The aim is to predict which classes of passengers of the TITANIC are more likely to survive the wreck. Those passengers are described by three predictive attributes: \( \text{Class} = \{1st; 2nd; 3rd; Crew\} \); \( \text{Age} = \{\text{Adult}; \text{Child}\} \); \( \text{Gender} = \{\text{Female}; \text{Male}\} \) and the attribute to predict \( \text{Survivor} = \{\text{No}; \text{Yes}\} \).

4 View-based method

4.1 Principle

In our first integrated method (?), the key idea is to associate each node in the decision tree with its corresponding relational view. In this method, the root node of the decision tree is represented by a relational view corresponding to the
Table 1  TITANIC database

<table>
<thead>
<tr>
<th>Class</th>
<th>Age</th>
<th>Gender</th>
<th>Survivor</th>
</tr>
</thead>
<tbody>
<tr>
<td>1st</td>
<td>Adult</td>
<td>Female</td>
<td>Yes</td>
</tr>
<tr>
<td>3rd</td>
<td>Adult</td>
<td>Male</td>
<td>Yes</td>
</tr>
<tr>
<td>2nd</td>
<td>Child</td>
<td>Male</td>
<td>Yes</td>
</tr>
<tr>
<td>3rd</td>
<td>Adult</td>
<td>Male</td>
<td>Yes</td>
</tr>
<tr>
<td>1st</td>
<td>Adult</td>
<td>Female</td>
<td>Yes</td>
</tr>
<tr>
<td>2nd</td>
<td>Adult</td>
<td>Male</td>
<td>No</td>
</tr>
<tr>
<td>1st</td>
<td>Adult</td>
<td>Male</td>
<td>Yes</td>
</tr>
<tr>
<td>Crew</td>
<td>Adult</td>
<td>Female</td>
<td>No</td>
</tr>
<tr>
<td>Crew</td>
<td>Adult</td>
<td>Female</td>
<td>Yes</td>
</tr>
<tr>
<td>2nd</td>
<td>Adult</td>
<td>Male</td>
<td>No</td>
</tr>
<tr>
<td>3rd</td>
<td>Adult</td>
<td>Male</td>
<td>No</td>
</tr>
<tr>
<td>Crew</td>
<td>Adult</td>
<td>Male</td>
<td>No</td>
</tr>
</tbody>
</table>

whole training dataset. Since each sub-node in the decision tree represents a sub-population of its parent node, we build for each node a relational view that is based on its parent view. Then, these views are used to count the frequency of each class in the node with simple GROUP BY queries. These counts are used to determine the criterion that helps either partitioning the current node into a set of disjoint sub-partitions based on the values of a specific attribute or concluding that the node is a leaf, i.e., a terminal node. To illustrate our method, we show in Figure 2 how these views are created based on the TITANIC training set (Table 1). Then we represent in Figure 3 the SQL statements for creating the views associated to the sample decision tree from Figure 2. This set of views constitutes the decision tree.

![Decision Tree Diagram](image)

**Figure 2**  TITANIC sample decision tree
Node #0: CREATE VIEW v0 AS SELECT Age, Gender, 
Class, Survivor 
FROM TITANIC 
Node #1.1: CREATE VIEW v11 AS SELECT Age, Class, Survivor FROM 
v0 WHERE Gender='Male' 
Node #1.2: CREATE VIEW v12 AS SELECT Age, Class, Survivor FROM 
v0 WHERE Gender='Female' 
Node #2.1: CREATE VIEW v21 AS SELECT Age, Survivor FROM v11 
WHERE Class='1st' 
Node #2.2: CREATE VIEW v22 AS SELECT Age, Survivor FROM v11 
WHERE Class='2nd'

Figure 3  Relational views associated with the TITANIC sample decision tree

4.2 Implementation

We present the algorithm for the ID3 method that we call View_ID3. We implemented this algorithm within the Oracle 10g DBMS as a PL/SQL stored procedure.

Algorithm.

Input parameters. The input parameters of our algorithm are given in Table 2.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Name</th>
<th>Default value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Data source table name</td>
<td>table_name</td>
<td>—</td>
</tr>
<tr>
<td>Class attribute (attribute to predict)</td>
<td>class</td>
<td>—</td>
</tr>
<tr>
<td>Result table name</td>
<td>res_name</td>
<td>BTRES</td>
</tr>
<tr>
<td>(Strict) minimum information gain for node building</td>
<td>min_gain</td>
<td>0</td>
</tr>
<tr>
<td>Root node view name</td>
<td>root_view</td>
<td>BTROOT</td>
</tr>
<tr>
<td>Clean-up views after execution (True/False)</td>
<td>del</td>
<td>TRUE</td>
</tr>
</tbody>
</table>

Table 2  View_ID3 Algorithm input parameters

Pseudo-code. We call a procedure named Entropy() that computes both the entropy and the frequency of a node. These data are used when computing the information gain. Entropy() is coded in PL/SQL. Our algorithm pseudo-code for the View_ID3 procedure is provided in Figure 4.

Result output. The output of our stored procedure, namely a decision tree, is stored into a relational table whose name is specified as an input parameter. The table structure reflects the hierarchical structure of the tree. Its fields are:

- node, the node ID number (primary key, the root node ID is always #0 — note that there is a direct link between the node ID and the associated view name);
- parent, the ID number of the parent node in the tree (foreign key, references a node ID number);
- rule, the rule that lead to the creation of this node, e.g., Gender='Female';
Create result table
Create root node using the data source table
Compute root node entropy and frequency
Push root node
Update result table with root node
While the stack is not empty do
  Pop current node
  Clean candidate list
  For each attribute but the class attribute do
    Create a new candidate
    For each possible value of current attribute do
      Build new node and associated relational view
      Compute new node entropy and frequency
      Update information gain
      Insert new node into current candidate node list
    End for (each value)
  End for (each attribute)
  Search for maximum information gain in candidate list
  For each candidate do
    If current attribute bears the greater information gain then
      For each node in the list of nodes do
        Push current node
        Update result table with current node
      End for (each node)
    Else
      For each node in the list of nodes do
        Destroy current node
      End for (each node)
    End if
  End for (each candidate)
End while (stack not empty)

Figure 4 Pseudo-code for ViewP3 stored procedure
- **frequency**, for each value V of attribute E, a field labeled \$E_V\$, the frequency for the considered value of the attribute in this node.

Such a table is best queried using Oracle SQL hierarchical statements. The result is directly a textual description of the output decision tree. A sample query is provided in Figure 5. From this representation, it is very easy to deduce the corresponding set of production rules.

```
SELECT LEVEL, node, parent, rule, E1, E2, ...
FROM btrees
CONNECT BY node = parent START WITH node = 0
```

**Figure 5** Hierarchical SQL query for decision tree display

5 **Contingency table-based method**

5.1 **Definition**

A contingency table is usually represented by means of a multidimensional table of frequencies that may contain NULL values. In our approach, data mining algorithms are integrated within DBMSs and hence operate onto relational data structures. In this context, contingency tables are represented by means of relational tables or views and contain only non NULL frequency values. This reduces considerably the size of the table. An additional attribute is then added to the contingency table structure to represent frequency values.

5.2 **Principle**

In this method (?), we aim at reducing the size of the initial training set in order to improve processing times. Thus, we build the contingency table, i.e., a table which contains the frequencies, corresponding to the whole training set. It can be computed by a simple SQL query. For example, let TS be a training set defined by \( n \) predictive attributes \( A_1, \ldots, A_n \) and the class attribute \( C \). The associated contingency table \( CT \) is obtained by executing the SQL query displayed in Figure 6.

```
CREATE VIEW CT_view AS
SELECT A1, \ldots, An, C, COUNT(*) AS Frequency
FROM TS
GROUP BY A1, \ldots, An, C
```

**Figure 6** Relational view associated to contingency table \( CT \)

Therefore, decision tree methods have to be adapted to be applied on this contingency table whose size is normally much smaller than the initial training set. Hence, the gain in terms of processing time is normally significant.
5.3 Running example and implementation

The classical contingency table corresponding to the TITANIC training set (Table 1) is provided in Figure 7. Its relational representation is obtained with a simple SQL query (Figure 8). Its result contains only 24 tuples (Figure 9).

<table>
<thead>
<tr>
<th></th>
<th>Adult</th>
<th></th>
<th>Child</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Male</td>
<td>Female</td>
<td>Male</td>
</tr>
<tr>
<td>1st</td>
<td>Yes</td>
<td>57</td>
<td>5</td>
</tr>
<tr>
<td></td>
<td>No</td>
<td>118</td>
<td>4</td>
</tr>
<tr>
<td>2nd</td>
<td>Yes</td>
<td>14</td>
<td>80</td>
</tr>
<tr>
<td></td>
<td>No</td>
<td>194</td>
<td>13</td>
</tr>
<tr>
<td>3rd</td>
<td>Yes</td>
<td>75</td>
<td>76</td>
</tr>
<tr>
<td></td>
<td>No</td>
<td>387</td>
<td>89</td>
</tr>
<tr>
<td>Crew</td>
<td>Yes</td>
<td>192</td>
<td>20</td>
</tr>
<tr>
<td></td>
<td>No</td>
<td>670</td>
<td>3</td>
</tr>
</tbody>
</table>

Figure 7 Classical contingency table for TITANIC

CREATE VIEW TITANIC_contingency AS
SELECT Class, Gender, Age, Survivor, COUNT(*) AS Frequency
FROM TITANIC
GROUP BY Class, Gender, Age, Survivor

Figure 8 Relational view associated to the TITANIC contingency table

We used Oracle 10g to implement our adaptation of ID3 to contingency tables, under the form of a PL/SQL stored procedure named CT_ID3.

5.4 New formula for the information gain

Since the training set is a contingency table (a table containing frequencies), this induces changes for computing the information gain for each predictive attribute, and consequently for computing the entropy.

To compute the information gain for a predictive attribute, our view-based ID3 implementation (View_ID3) reads all the tuples in the whole partition corresponding to the current node of the decision tree, in order to determine the tuple distribution regarding the values of each predictive attribute and the class attribute. In our contingency table-based method, it is quite simple to obtain the size of a subpopulation satisfying a given set of rules $E_r$ (e.g., Age = 'Child' AND Gender = 'Female') by summing the values of the Frequency attribute from the contingency table, for the tuples that satisfy $E_r$. Hence, we reduce the number of read operations to one only to compute the information gain for a predictive attribute. Indeed, as presented in section 3, the usual calculation of the information gain for an attribute having $k$ possible values and with a class attribute having $c$ possible values is:

$$G(S_K) = h_j(s_j) - \sum_{k=1}^{K} \left( \frac{n_k}{n_j} \times \left( -\sum_{i=1}^{c} \frac{n_{ik}}{n_k} \times \log_2 \left( \frac{n_{ik}}{n_k} \right) \right) \right)$$

(4)
<table>
<thead>
<tr>
<th>Class</th>
<th>Age</th>
<th>Gender</th>
<th>Survivor</th>
<th>Frequency</th>
</tr>
</thead>
<tbody>
<tr>
<td>1st Adult</td>
<td>Male</td>
<td>Yes</td>
<td>57</td>
<td></td>
</tr>
<tr>
<td>1st Adult</td>
<td>Male</td>
<td>No</td>
<td>118</td>
<td></td>
</tr>
<tr>
<td>1st Adult</td>
<td>Female</td>
<td>Yes</td>
<td>140</td>
<td></td>
</tr>
<tr>
<td>1st Adult</td>
<td>Female</td>
<td>No</td>
<td>4</td>
<td></td>
</tr>
<tr>
<td>1st Child</td>
<td>Male</td>
<td>Yes</td>
<td>5</td>
<td></td>
</tr>
<tr>
<td>1st Child</td>
<td>Female</td>
<td>Yes</td>
<td>1</td>
<td></td>
</tr>
<tr>
<td>2nd Adult</td>
<td>Male</td>
<td>Yes</td>
<td>14</td>
<td></td>
</tr>
<tr>
<td>2nd Adult</td>
<td>Male</td>
<td>No</td>
<td>154</td>
<td></td>
</tr>
<tr>
<td>2nd Adult</td>
<td>Female</td>
<td>Yes</td>
<td>80</td>
<td></td>
</tr>
<tr>
<td>2nd Adult</td>
<td>Female</td>
<td>No</td>
<td>13</td>
<td></td>
</tr>
<tr>
<td>2nd Child</td>
<td>Male</td>
<td>Yes</td>
<td>11</td>
<td></td>
</tr>
<tr>
<td>2nd Child</td>
<td>Female</td>
<td>Yes</td>
<td>13</td>
<td></td>
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<tr>
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<td>89</td>
<td></td>
</tr>
<tr>
<td>3rd Child</td>
<td>Male</td>
<td>Yes</td>
<td>13</td>
<td></td>
</tr>
<tr>
<td>3rd Child</td>
<td>Male</td>
<td>No</td>
<td>35</td>
<td></td>
</tr>
<tr>
<td>3rd Child</td>
<td>Female</td>
<td>Yes</td>
<td>14</td>
<td></td>
</tr>
<tr>
<td>3rd Child</td>
<td>Female</td>
<td>No</td>
<td>14</td>
<td></td>
</tr>
<tr>
<td>Crew Adult</td>
<td>Male</td>
<td>Yes</td>
<td>192</td>
<td></td>
</tr>
<tr>
<td>Crew Adult</td>
<td>Male</td>
<td>No</td>
<td>670</td>
<td></td>
</tr>
<tr>
<td>Crew Adult</td>
<td>Female</td>
<td>Yes</td>
<td>20</td>
<td></td>
</tr>
<tr>
<td>Crew Adult</td>
<td>Female</td>
<td>No</td>
<td>3</td>
<td></td>
</tr>
</tbody>
</table>

Figure 9  Relational representation of the TITANIC contingency table

where \( n_j \) is the node frequency, \( n_k \) is the frequency of the subnode having value \( V_k \) for the predictive attribute, \( n_{ik} \) is the frequency of the subnode partition having value \( V_k \) for the predictive attribute and value \( C_i \) for the class attribute. However, if we develop Formula 4, and since \( \log_2 \frac{n_j}{n_k} = \log_2 a - \log_2 b \), by adding up \( n_{ik} \) and \( n_k \), we obtain:

\[
G(S_K) = h_s(s_j) + \frac{1}{n_j} \times \left( \sum_{k=1}^{K} \sum_{i=1}^{c} n_{ik} \times \log_2 n_{ik} - \sum_{k=1}^{K} n_k \times \log_2 n_k \right) \tag{5}
\]

By applying Formula 5 to the contingency table (that we read only once), we obtain the information gain easily. Indeed, in this formula, it is not necessary to know at the same time various frequencies \( (n_j, n_k, n_{ik}) \), and we obtain \( n_k \) by summing the \( n_{ik} \) and \( n_j \) by summing the \( n_k \).

5.5 Complexity study

Our objective here is to compare the complexity of both our integrated methods (CT-ID3 and View-ID3) in terms of processing times. We suppose that both algorithms are optimized in their implementation so that only the necessary tuples are read. In this study, we are interested in the time spent reading and writing
data, since these are the most expensive operations. We consider that a tuple is read or written in one time unit. Finally, we consider that the obtained decision tree is balanced and whole, i.e., that at each level of the tree, the union of the populations of the various nodes equals the whole database.

Let \( N \) be the total number of tuples in the training set. Let \( K \) be the number of predictive attributes. Let \( T \) be the size of the corresponding contingency table.

With ViewJD3, to reach level \( i + 1 \) from an unspecified level \( i \) of the tree, each node must be read as many times as there are predictive attributes at this level, i.e., \( (K - i) \). As the sum of the frequencies at this level corresponds to the frequency of the starting database, it is thus necessary to read \( N \) tuples \( (K - i) \) times (number of tuples \( \times \) size of a tuple \( \times \) number of attributes). Hence, the total reading time for level \( i \) is \( N(K - i) \). In order to reach this level, it is also necessary to write the corresponding tuples. The writing time is thus \( N \).

Since \( \sum_{i=1}^{K-1} i = K(K + 1)/2 \), we obtain the following final complexity, from the root to the leaves (level \( K \)):
- reading complexity: \( N(K^2/2 - K/2) \) time units, therefore \( NK^2 \);
- writing complexity: \( NK \) time units.

In our contingency table-based method, we first create the contingency table. The writing time is thus \( T \). To compute the contingency table, we read the whole database once. The reading time is thus \( N \). When reaching level \( i + 1 \) from level \( i \), we read all the \( T \) tuples \( (K - i) \) times, for a total time by level of \( T(K - i) \).

Hence, with CTJD3, the complexity results are:
- reading complexity: \( T(K^2/2 - K/2) + N \) time units, therefore \( TK^2 \) or \( N \) if \( N > TK^2 \);
- writing complexity: \( T \) time units.

In conclusion, in terms of processing times, our contingency table-based method allows an improvement of \( N/T \) or \( K^2 \) (if \( N > TK^2 \)) for reading, and of \( NK/T \) for writing. Since \( N \) is usually much greater than \( T \), this improvement is significant.

6 Bitmap index-based method

6.1 Principle

Bitmap indices improve the performance of SQL queries including COUNT or bit-wise operations by not accessing source data. This type of queries is similar to those we need to build a decision tree and more precisely to define the size of the nodes’ sub-populations. Indeed, as we are going to explain next, in Table 4, to find the total number of “male survivors”, the SQL engine performs logical AND and COUNT operators onto bitmap indices and retrieves the result without accessing source data. In the case of a decision tree-based method, this query may correspond to a splitting step for obtaining the frequency of class \( \text{Survivor} = 'Yes' \) in the node corresponding to the rule \( \text{Gender} = 'Male' \). Our key idea comes from this very definition (?).
Table 3  Survivor bitmap index

<table>
<thead>
<tr>
<th>RowId</th>
<th>12</th>
<th>11</th>
<th>10</th>
<th>9</th>
<th>8</th>
<th>7</th>
<th>6</th>
<th>5</th>
<th>4</th>
<th>3</th>
<th>2</th>
<th>1</th>
</tr>
</thead>
<tbody>
<tr>
<td>Survivor</td>
<td>No</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>Yes</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
</tbody>
</table>

Table 4  Bitmap(Survivor=’Yes’) AND Bitmap(Gender=’Male’)

<table>
<thead>
<tr>
<th>RowId</th>
<th>12</th>
<th>11</th>
<th>10</th>
<th>9</th>
<th>8</th>
<th>7</th>
<th>6</th>
<th>5</th>
<th>4</th>
<th>3</th>
<th>2</th>
<th>1</th>
</tr>
</thead>
<tbody>
<tr>
<td>Survivor=’Yes’</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>Gender=’Male’</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>1</td>
<td>0</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>0</td>
</tr>
<tr>
<td>AND</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>0</td>
</tr>
</tbody>
</table>

6.2 Bitmap indices

Originally, a bitmap index is a data structure used to efficiently access large databases (7, 8). Generally, the purpose of an index is to provide pointers to the rows in a table that contain a given key value. In a regular index, this is achieved by storing a list of row identifiers (RowIds) for each key corresponding to the rows with that key value. In a bitmap index, records in a table are assumed to be numbered sequentially from 1. For each key value, a bitmap (array of bits) is used instead of a list of RowIds. Each bit in the bitmap corresponds to a possible RowId. If the bit is set to “1”, the row with the corresponding RowId contains the key value; otherwise the bit is set to “0”. A mapping function converts the bit position to an actual RowId, so the bitmap index provides the same functionality as a regular index even though it internally uses a different representation.

Example.

To illustrate how bitmap indices work, we use as an example the TITANIC database presented in Table 1. A bitmap index on the Survivor attribute is presented in Table 3.

Properties.

Bitmap indices are designed for efficient queries on multiple keys. Hence, queries are answered using bit-wise operations such as intersection (AND) and union (OR). Each operation exploits two bitmaps of the same size and is applied on corresponding bits to get the result bitmap. Every “1” bit in the result marks the desired tuple. Counting the number of tuples in the result is even faster. For queries such as “SELECT COUNT()...WHERE ... AND ... OR ...”, the logical operations can provide answers without accessing the source data.

In addition to standard operations, the SQL engine can use bitmap indices to efficiently perform special set-based operations using combinations of multiple indices, without accessing source data. For example, to find the total number of “male survivors”, the SQL engine can simply perform a logical AND operator between bitmaps Survivor = ’Yes’ and Gender=’Male’, and then count the number of “1” in the result bitmap (Table 4). Hence, 367 men survived the shipwreck. Note that, to obtain the result, the SQL engine does not require to browse the TITANIC table.
Table 5  Bitmap indices for the TITANIC database

<table>
<thead>
<tr>
<th></th>
<th>12</th>
<th>11</th>
<th>10</th>
<th>9</th>
<th>8</th>
<th>7</th>
<th>6</th>
<th>5</th>
<th>4</th>
<th>3</th>
<th>2</th>
<th>1</th>
</tr>
</thead>
<tbody>
<tr>
<td>Class</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Crew</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>1st</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>1</td>
</tr>
<tr>
<td>2nd</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>3rd</td>
<td>1</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>1</td>
<td>0</td>
</tr>
<tr>
<td>Age</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Child</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>Adult</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>0</td>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>Gender</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Female</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>1</td>
</tr>
<tr>
<td>Male</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>1</td>
<td>0</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>0</td>
</tr>
<tr>
<td>Survivor</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>No</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>Yes</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
</tbody>
</table>

6.3 Bitmap indices for building decision trees

In order to build decision trees using bitmap indices, for an initial training set, we create its associated set of bitmap indices for both the predictive attributes and the class attribute. For the root node of the decision tree, the frequency of each class is obtained by simply counting the total number of “1” values in the corresponding bitmap. For each other node in the decision tree, we compute a new set of bitmaps, each one corresponding to a class in the node. The bitmap characterizing each class in the current node is obtained by applying the AND operator between the bitmap associated to the node and the bitmaps corresponding to the successive related nodes from the root to the current node. To compute the frequency of each class in this node, we count the total number of “1” in the result bitmap. Since the information gain is based on population frequencies, it is also computed with bitmap indices.

6.4 Running Example

To illustrate our method, let us take as an example the TITANIC database presented in Table 1.

For each predictive attribute and the class attribute, we create its corresponding bitmap index (Table 5). Thus, our new learning population is precisely composed of these four bitmap indices. Hence, we apply the decision tree building method directly on this set of bitmap indices instead of the whole TITANIC database.

To build the root node of the decision tree, we just have to determine the frequency of each class. In our running example, the class attribute Survivor has two possible values: ‘Yes’ or ‘No’. Thus, we have to determine two sub-populations, one for Survivor=‘Yes’ and the other for Survivor=‘No’ from the bitmap index of the Survivor attribute (Table 3). The frequency of each class in the Survivor attribute is obtained by counting the number of “1” in the bitmap associated to Survivor=‘Yes’ and in the bitmap associated to Survivor=‘No’, respectively (Fig. 10).
Table 6  \(A&D\_b\_i\_t\_m\_a\_s\) for the node \textit{Gender} = 'Male'

<table>
<thead>
<tr>
<th>RowId</th>
<th>12</th>
<th>11</th>
<th>10</th>
<th>9</th>
<th>8</th>
<th>7</th>
<th>6</th>
<th>5</th>
<th>4</th>
<th>3</th>
<th>2</th>
<th>1</th>
</tr>
</thead>
<tbody>
<tr>
<td>\textit{Survivor}='Yes'</td>
<td>.0</td>
<td>.0</td>
<td>.0</td>
<td>.1</td>
<td>.0</td>
<td>.1</td>
<td>.0</td>
<td>.1</td>
<td>.0</td>
<td>.1</td>
<td>.0</td>
<td>.0</td>
</tr>
<tr>
<td>\textit{Gender}='Male'</td>
<td>.1</td>
<td>.1</td>
<td>.1</td>
<td>.0</td>
<td>.1</td>
<td>.1</td>
<td>.0</td>
<td>.1</td>
<td>.1</td>
<td>.0</td>
<td>.1</td>
<td>.0</td>
</tr>
<tr>
<td>\textit{AND}</td>
<td>.0</td>
<td>.0</td>
<td>.0</td>
<td>.0</td>
<td>.1</td>
<td>.0</td>
<td>.0</td>
<td>.1</td>
<td>.1</td>
<td>.0</td>
<td>.1</td>
<td>.0</td>
</tr>
<tr>
<td>\textit{Survivor}='No'</td>
<td>.1</td>
<td>.1</td>
<td>.1</td>
<td>.0</td>
<td>.1</td>
<td>.0</td>
<td>.0</td>
<td>.0</td>
<td>.0</td>
<td>.0</td>
<td>.0</td>
<td>.0</td>
</tr>
<tr>
<td>\textit{Gender}='Male'</td>
<td>.1</td>
<td>.1</td>
<td>.1</td>
<td>.0</td>
<td>.1</td>
<td>.1</td>
<td>.0</td>
<td>.1</td>
<td>.1</td>
<td>.0</td>
<td>.1</td>
<td>.0</td>
</tr>
<tr>
<td>\textit{AND}</td>
<td>.1</td>
<td>.1</td>
<td>.1</td>
<td>.0</td>
<td>.0</td>
<td>.0</td>
<td>.1</td>
<td>.0</td>
<td>.0</td>
<td>.0</td>
<td>.0</td>
<td>.0</td>
</tr>
</tbody>
</table>

The variation of entropy indicates that the splitting attribute is \textit{Gender}. This attribute has two possible values 'Female' and 'Male'. The population of the current node is then divided into two sub-nodes corresponding to the rules \textit{Gender} = 'Male' and \textit{Gender} = 'Female', respectively. Each sub-node is composed of two sub-populations that survived or not. To obtain the sizes of these sub-populations, we apply the logical operator \textit{AND} firstly between the \textit{Gender} = 'Male' and the \textit{Survivor} = 'Yes' bitmaps and secondly between the \textit{Gender} = 'Male' and the \textit{Survivor} = 'No' bitmaps, as shown in Table 6.

To obtain the frequency of the sub-population associated to the rule “ \textit{Survivor} = 'Yes' AND \textit{Gender} = 'Male' ” (respectively “ \textit{Survivor} = 'No' AND \textit{Gender} = 'Male' ”), we simply count the total number of “1” in the corresponding \textit{AND bitmap} (Table 6). The same process is applied for the node corresponding to the rule \textit{Gender} = 'Female' (Fig. 11).

The variation of entropy now indicates that the next splitting attribute is \textit{Class}. From the node \textit{Gender} = 'Male', we obtain four sub-nodes, since the \textit{Class} attribute
Table 7: \textit{AND bitmaps} associated to the node corresponding to the rule \textit{Class='1st'}

<table>
<thead>
<tr>
<th>RowId</th>
<th>12</th>
<th>11</th>
<th>10</th>
<th>9</th>
<th>8</th>
<th>7</th>
<th>6</th>
<th>5</th>
<th>4</th>
<th>3</th>
<th>2</th>
<th>1</th>
</tr>
</thead>
<tbody>
<tr>
<td>\textit{Survivor='Yes'} AND \textit{Gender='Male'}</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>1</td>
<td>0</td>
<td></td>
</tr>
<tr>
<td>\textit{Class='1st'} AND \textit{Gender='Male'}</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td></td>
</tr>
<tr>
<td>\textit{AND}</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td></td>
</tr>
<tr>
<td>\textit{Survivor='No'} AND \textit{Gender='Male'}</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td></td>
</tr>
<tr>
<td>\textit{Class='1st'} AND \textit{Gender='Male'}</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td></td>
</tr>
<tr>
<td>\textit{AND}</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td></td>
</tr>
</tbody>
</table>

has four values (‘1st’, ‘2nd’, ‘3rd’ and ‘Crew’). For example, to obtain the frequencies of the sub-populations corresponding to the node \textit{Class='1st'}, we compute two \textit{AND bitmaps}, namely (\textit{Gender='Male'} AND \textit{Class='1st'} AND \textit{Survivor='Yes'}) and (\textit{Gender='Male'} AND \textit{Class='1st'} AND \textit{Survivor='No'}) (Table 7). The sub-populations’ frequencies are then obtained by counting the total number of “1” in each obtained \textit{AND bitmap}.

6.5 Implementation

The implementation of the ID3 method using bitmap indices takes the form of a PL/SQL stored procedure named \textit{Bitmap_ID3} under Oracle 10g. This stored procedure allows us to create the necessary bitmap indices for a given training set and then to build the decision tree. Since Oracle uses B-Tree indices by default, we forced it to use bitmap indices. The nodes of the decision tree are built by using an SQL query that is based on an \textit{AND} operation applied on its own bitmaps and its parent bitmaps. Then, the obtained \textit{AND bitmaps} are used to count the population frequency of each class in the node with simple COUNT queries. These counts are used to determine the criterion that helps either partitioning the current node into a set of disjoint sub-partitions based on the values of a specific attribute or concluding that the node is a leaf, i.e., a terminal node. Similarly, to compute the information gain for a predictive attribute, our implementation uses bitmap indices rather than the whole training set.

6.6 Complexity study

Our objective here is to confirm, from a theoretical point of view, the gain induced by considering the set of bitmap indices rather than the initial training set as the learning set (we denote them respectively bitmap index-based method and classical method). For this study we place ourselves in the worst case, i.e., the indices are too large to be loaded in main memory.

Let \( N \) be the total number of tuples in the training set, \( K \) the number of attributes, \( L \) the average length, in bits, of each attribute and \( A \) the average number of values of each attribute.
First we evaluate the size of training sets. The size of the initial training set \( N \ast L \ast K \) bits. For our bitmap index-based method, this initial training set is replaced by the set of bitmap indices. Thus \( K \) bitmap indices are created with an average number of \( A \) bits per index. Each bitmap has a size of \( N \) bits. In this case, the size of the training set is \( N \ast A \ast K \) bits. As regards to the size of the training set and thus the loading time, our method is preferable if \( A < L \), which corresponds to a majority of cases.

In terms of data reading time, we consider that a bit is read in one time unit. The total number of nodes on the \( i \)-th depth level can be approximated by \( A^{i-1} \). Indeed we suppose that the obtained decision tree is complete and balanced. To reach level \( i + 1 \) from an unspecified level \( i \) of the tree, each training set must be read as many times as there are predictive attributes remaining at this level, i.e., \( (K - i) \).

In the classical method, as the size of the training set is \( N \ast L \ast K \), reading time for level \( i \) (in time units) is \( (K - i) \ast N \ast L \ast K \ast A^{i-1} \). Hence, to build the whole decision tree, in the classical method, the reading time is : \( \sum_{i=1}^{K} (K - i) \ast N \ast L \ast K \ast A^{i-1} \).

In our bitmap index-based method, the index size is approximated by \( N \ast A \) bits. To reach level \( i + 1 \) from an unspecified level \( i \) of the tree, for a given predictive attribute, the number of index to read is \( i + 1 \). Thus, at level \( i \), the reading time is : \( (i + 1)(K - i)N \ast A^{i} \). Hence, to build the whole decision tree with our bitmap index-based method, the reading time is : \( \sum_{i=1}^{K} (i + 1)(K - i)N \ast A^{i} \).

To evaluate the gain in time, we build the following ratio :

\[
R = \frac{\text{time with classical method}}{\text{time with bitmap index-based method}} = \frac{\sum_{i=1}^{K} (K - i) \ast N \ast L \ast K \ast A^{i-1}}{\sum_{i=1}^{K} (i + 1)(K - i)N \ast A^{i}}.
\]

After computing we obtain : \( R = \frac{\sum_{j=0}^{K} (K-j) \ast A^{j}}{\sum_{j=0}^{K} (j+1) \ast A^{j}} = \frac{1}{K} (1 + G) \)

As we consider the polynomials of higher degree, \( G \) is of complexity \( K \). Thus \( R^{-1} \) is of complexity \( \frac{1}{K} \). Indeed \( R^{-1} = \frac{1}{\frac{1}{K} (1 + K)} = \frac{1}{K} (1 + \frac{1}{K}) \) and \( \frac{1}{K} \) is insignificant. Our method is interesting if the ratio \( R^{-1} \) is lower than one, that means if \( A < L \), which corresponds to a majority of the cases.

7 Performance

In order to validate our integrated implementation of data mining methods and to compare its performance with an in-memory implementation, we carried out tests on different views from the CovType database\(^8\). The CovType database contains 581,012 tuples defined by 54 predictive attributes and one class (with seven distinct values). We created five views, each one containing a part of the Covtype database, and defined by three predictive attributes (each one having five values) and the class. The predictive attributes we used and the size of each view are provided in Figure 12. These tests have been performed on a PC computer with 1.50GHz and 512 MB of RAM running the Personal Oracle DBMS version 10g.

Figure 13 shows the results achieved with our different implementations of ID3. The classical, in-memory method using the Sipina software (\( ? \)), the view-based, the

\(^8\)http://r.ids.uci.edu/pub/machine-learning-databases/covtype/
contingency table-based and the bitmap index-based implementations are respectively labeled SimaJD3, ViewJD3, CTJD3 and BitmapJD3. For integrated approaches, we add to processing time the time required for building bitmap indices and the contingency table. In opposition, processing time with SimaJD3 includes loading time, since it is necessary to load the data from the database into the memory each time the algorithm is executed.

First of all, we note that for databases larger than 2.270 MB, with the hardware configuration used for the tests, Sima is unable to build the decision tree, whereas our integrated methods can. Sima is indeed limited by the size of the memory.

Moreover, our results clearly underline the gain induced by our integrated approach, compared to the classical in-memory approach. The processing time for SimaJD3 indeed increases from about sixteen to eighty seconds when the view size is multiplied by five. Thus, the processing time for SimaJD3 is multiplied by about five, whereas it is multiplied by three for view-based and bitmap index-based methods, and by a little more than one for the contingency table-based method.

Now, if we compare our different integrated methods, processing time increases more smoothly. The processing time increase is almost identical for ViewJD3 and BitmapJD3 (from about nine to twenty-two seconds for ViewJD3, and from about five to sixteen seconds for BitmapJD3). Processing time for CTJD3 is almost constant (from about 2 to 3 seconds).

Our experimental results also demonstrate that the contingency table-based method is the best integrated method. For CTJD3, the induced gain mainly depends on the size of the contingency table, which is generally considerably smaller than the size of the initial training set. Nevertheless, in extreme cases, the size of the contingency table may be so close to that of the whole training set that the profit becomes negligible. However, this is very rare in real-life cases and scanning the contingency table can never be worse than scanning the whole database.

ViewJD3 is the slowest integrated method. In this case, processing times remain quite long because of multiple accesses to the database, because it does not use any optimization tool. The bitmap index-based method is about 30% faster than ViewJD3 on an average. This result was expected since using bitmap indices avoids many data accesses.

Finally, we can say that our integrated methods are particularly interesting for large databases. Sima is indeed very fast for computing and very slow for loading data, whereas our integrated methods bear the opposite behavior: and loading time increases quicker than computing time when the database grows larger. The

<table>
<thead>
<tr>
<th>View name</th>
<th>Predictive attributes used</th>
<th>View size (in tuples)</th>
<th>View size (in MB)</th>
</tr>
</thead>
<tbody>
<tr>
<td>view1</td>
<td>1, 2, 3</td>
<td>116202</td>
<td>454</td>
</tr>
<tr>
<td>view2</td>
<td>4, 5, 6</td>
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<td>908</td>
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<td>view3</td>
<td>7, 8, 9</td>
<td>348607</td>
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<tr>
<td>view4</td>
<td>1, 4, 10</td>
<td>464810</td>
<td>1816</td>
</tr>
<tr>
<td>view5</td>
<td>2, 5, 8</td>
<td>581012</td>
<td>2270</td>
</tr>
</tbody>
</table>

Figure 12 Views used in CovType tests
use of a contingency table as an optimization tool improves processing times the most significantly.

![Performance comparison of ID3 implementations](image)

Figure 13 Performance comparison of ID3 implementations

8 Conclusion and perspectives

In order to apply data mining algorithms to large databases, two main approaches are proposed in the literature: the classical approach and the integrated approach. The classical approach is limited by the size of the processed databases, since it exploits separate data mining pieces of software that operate in main memory. The main objective in this approach is then to reduce the size of databases, either by using techniques for preprocessing data or by sampling. The integrated approach consists in processing data mining methods within DBMSs using only the tools offered by these systems. By exploiting their management of persistent data, the database size limit is topped.

Following the integrated approach, we proposed in this paper a framework to offer to DBMS users on-line data mining operators for mining large databases without size limit and in acceptable processing times. We proposed three integrated methods (a view-based method, a contingency table-based method and a bitmap index-based method) for applying decision tree algorithms on large databases. Each method is based on a specific database tool, namely relational views, contingency table and bitmap indices, respectively.

To validate our on-line data mining approach, we have implemented three decision tree building methods (ID3, C4.5, CART)\(^b\) under Oracle 10g, as a PL/SQL package named `decision_tree` that is available on-line \(^c\).

Moreover, we carried out tests on different data sets to compare our different integrated methods with the classical, in-memory method. Our experimentation clearly underlined the efficiency of our integrated methods when the database is large. We showed that we could process very large databases without any size limit, while Sipina could not. In addition, we showed that our contingency table-based method presented the best processing time. This result could be expected

\(^a\)In this paper, we have detailed the algorithm and results only for the ID3 method.

\(^b\)http://bdd.univ-lyon2.fr/download/decision_tree.zip
since it is based on aggregated data that reduce the size of the initial training set. Note that in-memory data mining methods could also use contingency tables instead of original learning sets to improve their processing time.

The perspectives opened by this study are numerous. First, we plan to add in the decision tree package other procedures to supplement the offered data mining tools, such as sampling, missing values management, learning validation techniques, and non-supervised learning methods.

We also aim to adapt our integrated approach to mine data warehouses since they can be stored as relational databases. For example, our contingency-table based method can be performed on relational data cubes by applying the SUM function.

Finally, most of data mining research has concentrated on the single table case. We are currently extending our integrated approach to deal with multiple relational tables. Our first idea consists in using bitmap join indices. Then, we can talk about on-line database mining, which incorporates the ability to access directly data stored in a database (several related tables) rather than on-line data mining (one single table).

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